

address, and phone  
 by present: only one  
 Ostriker (M442)  
 Univ. Med. Ctr.  
 Ave.  
 NY 10016

ence  
 poster  slide  
 indicate preference if  
 not available:  
 alternative  
 only  
 abstract

and topics.  
 one theme and one  
 for programing and  
 paper.  
 e: G  
 SMS ....  
 title: 07  
 system

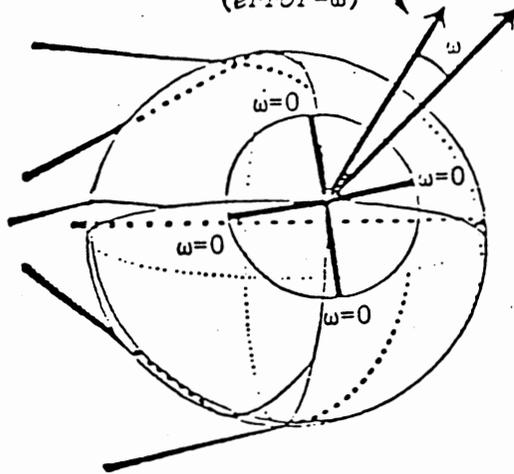
g., for sequential

Tensor Network Theory Applied to the Oculomotor System. CNS Activity Expressed with Natural, Non-Orthogonal Coordinates. G. Ostriker, A. Pellionisz and R. Llinas. Dept. Physiology and Biophysics, New York Univ. Med. Ctr., 550 First Ave., NY 10016.

Nature often provides inherently oblique systems of coordinates, where Cartesian conventions are not valid. The extra-ocular motor system is an example of a geometry in which the intrinsic frame of reference is clearly non-orthogonal. Previous models (Robinson, Boeder) have defined the positional parameters of the extra-ocular muscles. It is apparent that a general approach to coordinate systems, such as tensor analysis, is needed. Expressing the above models with this method, applicable to any coordinate system, the implications of non-orthogonality and an overcomplete number of axes can be revealed naturally.

While an eye movement is a physical invariant, we describe it vectorially in "oculomotor hyperspace" by either covariant or contravariant components. By definition, movement arises through the physical summation of contravariant vector components. However, if the CNS were to relay intention (covariant) vectors directly to the extraocular muscles, the degree of accuracy in the production of intended movements would be a measure of the orthogonality of the system. For saccadic

execution of contravariants  
 (on target)  
 execution of covariants  
 (error= $\omega$ )



eye movements we work with two coordinate systems, one based upon the actual length changes of the six extraocular muscles and their axes of rotation, and another which is a projection of the first system onto a tangent plane. We characterize saccadic eye movements (from primary, secondary, and tertiary positions) by both covariant and contravariant components. Allowing covariant vectors to be relayed to the muscles (as if they were contravariants), this movement will differ from the original direction by an "error" angle  $\omega$ , as shown.

Orthogonality would result in eigenvectors (defined by  $\omega=0$ ) in all directions. Our results show that the execution of covariants leads to an error in every direction except for the four eigenvectors of the system. Supported by Grant NS13742.

Do not type on or past blue lines (printer's cut lines).

for Neuroscience member required below. No member may sign more than one abstract.

Member certifies that any work with human or animal subjects related in this abstract complies with the guiding principles for procedures endorsed by the Society.

G. Ostriker

Neuroscience member's signature

Printed or typed name

212/340-5410

Telephone number

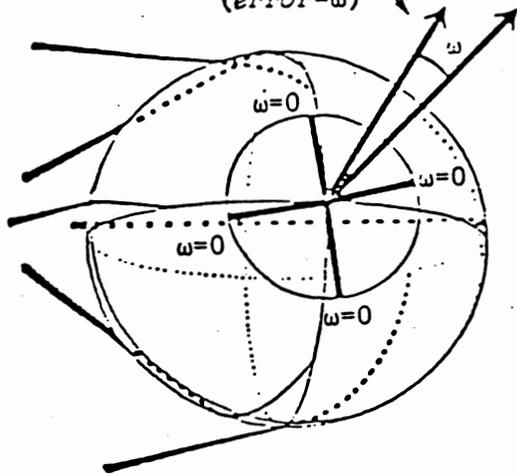
**TENSOR NETWORK THEORY APPLIED TO THE OCULOMOTOR SYSTEM. CNS ACTIVITY EXPRESSED WITH NATURAL, NON-ORTHOGONAL COORDINATES. G. Ostriker, A. Pellionisz and R. Llinas. Dept. Physiology and Biophysics, New York Univ. Med. Ctr., 550 First Ave., NY 10016.**

Nature often provides inherently oblique systems of coordinates, where Cartesian conventions are not valid. The extra-ocular motor system is an example of a geometry in which the intrinsic frame of reference is clearly non-orthogonal. Previous models (Robinson, Boeder) have defined the positional parameters of the extra-ocular muscles. It is apparent that a general approach to coordinate systems, such as tensor analysis, is needed. Expressing the above models with this method, applicable to any coordinate system, the implications of non-orthogonality and an overcomplete number of axes can be revealed naturally.

While an eye movement is a physical invariant, we describe it vectorially in "oculomotor hyperspace" by either covariant or contravariant components. By definition, movement arises through the physical summation of contravariant vector components. However, if the CNS were to relay intention (covariant) vectors directly to the extraocular muscles, the degree of accuracy in the production of intended movements would be a measure of the orthogonality of the system. For saccadic

*execution of contravariants*  
 (on target)

*execution of covariants*  
 (error= $\omega$ )



eye movements we work with two coordinate systems, one based upon the actual length changes of the six extraocular muscles and their axes of rotation, and another which is a projection of the first system onto a tangent plane. We characterize saccadic eye movements (from primary, secondary, and tertiary positions) by both covariant and contravariant components. Allowing covariant vectors to be relayed to the muscles (as if they were contravariants), this movement will differ from the original direction by an "error" angle  $\omega$ , as shown.

Orthogonality would result in eigenvectors (defined by  $\omega=0$ ) in all directions. Our results show that the execution of covariants leads to an error in every direction except for the four eigenvectors of the system. Supported by Grant NS13742.